

A voltage sensitivity index application for power system load shedding considering the generator controls

L T Nghia¹, T T Giang¹, Q H Anh¹, P T T Binh², N T An¹, P H Hau¹

¹Department of Electrical and Electronics Engineering, HCMC University of Technology and Education, Vietnam

Email: trongnghia@hcmute.edu.vn

²Department of Electrical and Electronics Engineering, HCMC University of Technology, Vietnam

Email: thanhbinh055@yahoo.com

Abstract—This paper proposes a method for calculating the minimum amount of power load needed to shed and distributing it for each load bus in order to recover the frequency and voltage back to the allowable range. Based on the consideration of the primary control of the turbine governor and the reserve power of the generators for secondary control, the minimum amount of load shedding was calculated in order to recover the frequency of the power system. Computation and analysis of Voltage Sensitivity Index (VSI) of the load bus to prioritize distribution of the amount power load shedding at these positions. The lower the load bus have the Voltage Sensitivity Index (VSI), the higher the amount of load shedding will shed and vice versa. With this technique, frequency and voltage value are still within allowable range, and a large amount of load shedding could be avoided, hence, saved from economic losses, and customer service interruption. The effectiveness of the proposed method tested on the IEEE 37 bus 9 generators power system standard has demonstrated the effectiveness of this method.

Keywords— Load shedding, Voltage Sensitivity Index (VSI), Frequency control, Primary control, Secondary control.

I. INTRODUCTION

The imbalance active power between the generation and the load demand causes a decrease the frequency in the power system. The monitoring and control system will immediately implement the control solutions to restore the frequency back to the allowable value, and improve the power system stability [1]. In [2], the primary and secondary control power plants are set by automatic controlled equipment or the power system operator. After implementing all possible control solutions that the system's frequency has not yet recovered to the allowable value, the most efficient method is to reduce the load [3]. The under-frequency load shedding relay (UFLS) is the traditional load shedding method used quite commonly in the current power system. In [4], the relays are set to operate whenever the frequency drops to a specified level and a fixed amount of load power is shed to restore the frequency. Using under frequency load shedding relay to disconnect the load bus will make in insufficient or excessive load shedding and take a long time to restore the frequency back to stable. This result will make damages for the suppliers and customers using the system's power. The authors in [5], [6] showed methods to estimate the

amount load shedding, which based on the frequency reduction, or the rate of change of frequency (ROCOF). The combination of Intelligent load shedding methods has also been studied and developed such as Artificial Neural Network (ANN) [7], fuzzy logic algorithms [8], genetic algorithm (GA) [9] or particle swarm optimization (PSO) algorithm. These methods minimize the load shedding costs at steady state operation of pow system [10], [11].

A good load shedding program should be shed with the minimum number of load buses and as quickly as possible, and must meet the system's permissible frequency conditions. On the other hand, in large disturbances of the power system, frequency decay is often associated with voltage decay. Voltage decay at load buses reduces system load, therefore the reduction in frequency is slowed and the actual load shedding by UFLS is reduced relative to the level required [12] - [14]. In most practical conditions, the amount of load shedding may be more or less the amount of power the system needs to maintain the frequency, which may lead to cost losses as well as affects the objects that the system serves.

This paper presents a new method of load shedding to minimize the amount of load shedding power. The load

shedding strategies based on the Voltage Sensitivity Index (VSI) to find out the priority and distribute the amount of load shedding power for each load bus. For load buses, the lower the load bus have the Voltage Sensitivity Index (VSI), the higher the amount of load shedding will shed and vice versa. er system [10], [11].

II. METHODOLOGY

2.1 Overview the power system frequency responds

The basic concepts of speed governing are best illustrated by considering an isolated generating unit supplying a local load as shown in Figure 1.

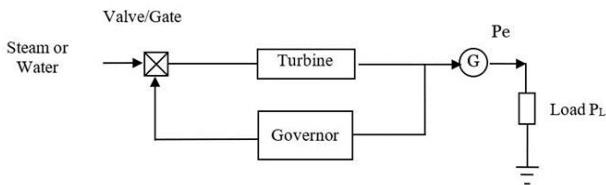


Fig. 1: Generator provides independent load

The power system loads are a composite of a variety of electrical devices. For resistive loads, such as lighting and heating loads, the electrical power is independent of frequency. In the case of motor loads, such as fans and pumps, the electrical power changes with frequency due to changes in motor speed. The references [15], [16] showed the overall frequency-dependent characteristic of a composite load:

$$\Delta P_e = \underbrace{\Delta P_L}_{\text{Nonfrequency-sensitive-load-change}} + \underbrace{D\Delta\omega}_{\text{Frequency-sensitive-load-change}} \quad (1)$$

where: ΔP_L - is the load component does not depend on frequency, eg heat load, lighting, ...; $D\Delta\omega$ - the change in load depends on the change of frequency, eg, motors, pumps, etc; ΔP_e Deviation of power change; $\Delta\omega$: Deviation of angle speed change; D: The percentage change in load with percentage of change in frequency varies, D is from 1 ÷ 2%.

The transfer function block diagram reflects the relationship between the load change and the frequency taking into account the governor characteristic, the prime mover and the load response shown in Figure 2 [17].

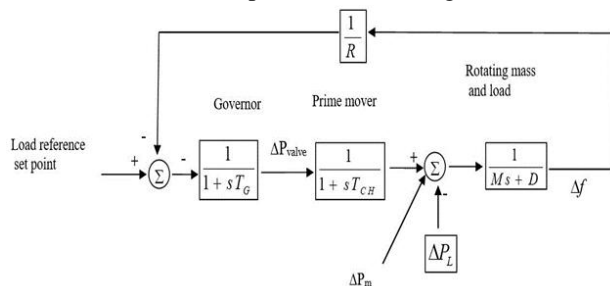


Fig. 2: The transfer function block diagram describes the relationship between the load changes and frequency

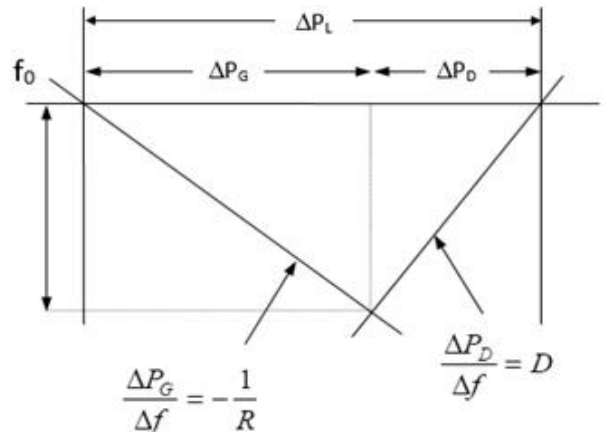


Fig. 3: The effects of the governor speed droop and the frequency of load on the net frequency [18].

The transfer function relating the load change, ΔP_L , to the frequency change, $\Delta\omega$, is

$$\Delta f(s) = \Delta P_L(s) \left[\frac{\frac{-1}{Ms+D}}{1 + \frac{1}{R} \left(\frac{1}{1+sT_G} \right) \left(\frac{1}{1+sT_{CH}} \right) \left(\frac{1}{Ms+D} \right)} \right] \quad (2)$$

Where: K_G the amplification stage; ω_{ref} reference speed;

T_{CH} “charging time” time constant; ΔP_{Valve} per unit change in valve position from nominal; Ms angular momentum of the machine in Laplace transform; R is equal to pu change in frequency divided by pu change in unit output; it is characteristic for the sliding speed adjustment; $R = -\Delta f / \Delta P$

The purpose of system simulation in the form of a transfer function is to calculate the time response of the frequency deviation when the load change step is ΔP_L . From the above description, frequency deviation in steady state it means the values of the transfer function is determined for $s = 0$:

The steady-state value of $\Delta f(s)$ may be found by:

$$\Delta f \text{ steady state} = \lim_{s \rightarrow 0} [s\Delta f(s)] = \frac{-\Delta P_L \left(\frac{1}{D} \right)}{1 + \left(\frac{1}{R} \right) \left(\frac{1}{D} \right)} = \frac{-\Delta P_L}{R + D} \quad (3)$$

When the power system has multiple generators with independent governors, the frequency deviation in steady state is calculated according to formula (4).

$$\Delta f = \frac{-\Delta P_L}{\frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_n} + D} \quad (4)$$

Set $\beta = \left(\frac{1}{R_{eq}} + D \right)^{-1}$ is the general frequency response

characteristic of power system. It includes the adjustment characteristics of turbine mechanical power and load. From formula (4), obtain:

$$\Delta f = -\Delta P_L \cdot \beta \tag{5}$$

2.2 Primary and secondary frequency control in the power system

Primary frequency control is an instantaneous adjustment process performed by a large number of generators with a turbine power control unit according to the frequency variation. Secondary frequency control is the subsequent adjustment of primary frequency control achieved through the AGC's effect (Automatic Generation Control) on a number of units specifically designed to restore the frequency back to its nominal value or otherwise, the frequency-adjusting effects are independent of the governor's response called the secondary frequency control. The process of the primary and secondary frequency control was shown in Figure 4.

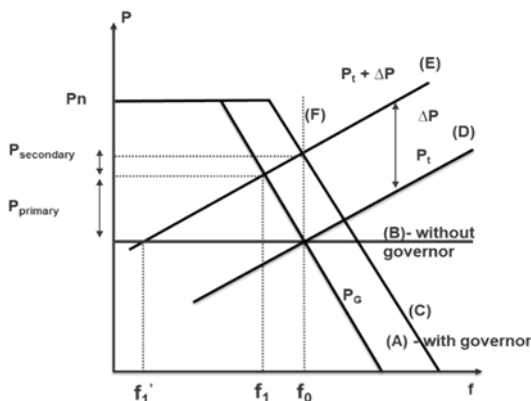


Fig. 4: The relationship between frequency deviation and output power deviation.

Characteristic line (A) shows the effect of the governors: change the turbine power according to the change of frequency:

In balance mode, the intersection of the generator characteristic line (A) with the frequency characteristic of the load line (D) determines the frequency f_0 equal 50Hz (or 60 Hz). When the load increases ΔP_L , the new characteristic line will be line (E): $P_t + \Delta P$. In addition, the intersection of the generator characteristic line (A) with the new load characteristic line (E) defines the new frequency f_1 . Here, $f_1 < f_0$. Compared to the case where the generator does not have a governor, characteristic line (B), it is clear that: $f_1 < f_0$. According to the characteristic line (A) of the generator unit, the governor does not prevent the frequency reduction: $\Delta f = f_0 - f_1$

However, because the generator has the governor, it has helped to limit the large deviation of the frequency. Compared with the case the generators do not have a governor (B), the intersection with the new characteristic line of the load (E) will determine the frequency f_1 : $f_1 < f_0$. Thus, the governor of the generator unit has the effect of reducing the large change of frequency known as the primary frequency controller. The efficiency of the primary frequency control depends on the slope of the speed-droop characteristic of the generator units. In the ideal case, the adjusting characteristic line (F) of the generator unit is vertical line; the frequency will not change until the power limit of the generator unit P_n .

The above characteristics of the primary adjustment process lead to the need for external intervention (by the automatic control device or by the power system operators) - that is the secondary frequency control process. The secondary adjustment characteristic is represented by the simultaneous shifting of the characteristic line (A) into the characteristic line (C) of the generator unit, with the slope unchanged. This adjustment is equivalent to the creation of a static vertical adjustment characteristic line (F). Thus, the secondary adjustment is within the rated power range of the generator unit to restore and maintain the frequency within the allowable value.

2.3 Calculate the minimum load shedding power considering the control characteristic of turbine mechanical power and load

In the 60Hz power system, the frequency deviation allowed Δf_p is 0.3 Hz ($\Delta f_p = -0.3\text{Hz}$). In the case of the power deficiency or imbalance between the source and the load causing the frequency difference, the frequency control will be implemented in the following order: primary control, secondary control. When the reserved power is used for secondary control and the frequency has not been restored to the permitted value, the load will be shed. Thus, from formula (5), the relationship between the permissible change in frequency, the amount of secondary control power and the minimum load shedding power P_{LSmin} is calculated according to the proposed formula below:

$$\Delta f_p = -\beta \cdot [\Delta P_L - (\Delta P_{\text{Secondary control}} + P_{LSmin})] \tag{6}$$

In this case, if $(\Delta P_{\text{Secondary control}} + P_{LSmin}) < \Delta P_{\text{Secondary max}}$, then $\Delta P_{LSmin} = 0$, otherwise the minimum power load shedding is calculated by the formula below:

$$P_{LSmin} = \Delta P_L - \left(\frac{-\Delta f_p}{\beta} \right) - \Delta P_{\text{Secondary Max}} \tag{7}$$

Where: Δf_p is the permissible change in frequency (pu); P_{LSmin} is the minimum amount of power required to shed

(pu); $\Delta P_{\text{Secondary control}}$ is the amount of secondary control power addition to the system.

2.4 The Voltage Sensitivity Index (VSI)

The main objective of calculating VSI is to find the most sensitive node of the system from voltage sensitivity point of view [19]. It considered a numerical solution, which helps operator to monitor how to shed the load to prevent frequency and voltage collapse. Nodes, having minimum voltage sensitivity index are selected and then, using equation (8) to calculate the voltage sensitivity index (VSI).

VSI at bus i, is defined as [20]:

$$VSI_i = \sqrt{\frac{\sum_{k=1}^n (1 - V_k)^2}{n}} \tag{8}$$

Where V_k is voltage at k^{th} node and n is the number of nodes.

After calculating the minimum amount of load shedding power required, the next issue determines the distribution the amount of load shedding power at load buses. The node with least VSI will be picked as the best location for the load shedding. That mean, the amount of load shedding at different load buses can be calculated in the same way as the principle of the load sharing in the parallel circuit.

Due to parallel electrical circuits:

$$Y = \frac{1}{Z_{eq}} = \frac{1}{Z_1} + \frac{1}{Z_2} + \dots + \frac{1}{Z_n} \tag{9}$$

$$Z_{eq} = \frac{1}{Y} \tag{10}$$

$$\frac{P_1}{P} = \frac{U^2}{Z_1} \cdot \frac{Z_{eq}}{U^2} = \frac{Z_{eq}}{Z_1} \tag{11}$$

Equivalent formula follows:

$$\frac{P_i}{P} = \frac{Z_{eq}}{Z_i} \square \frac{VSI_{eq}}{VSI_i} \tag{12}$$

Here, the general formula calculates the amount of load shedding distribution at nodes according to the Voltage

Sensitivity Index (VSI): $P_{LSi} = \frac{VSI_{eq}}{VSI_i} \cdot P_{LS\min}$ (13)

Where, n is the number of generator bus; i is the number of load bus; P_{LSi} the amount of load shedding power for the i bus (MW); $P_{LS\min}$ the minimum amount of load shedding power to the restore of frequency back to the allowable value (MW); VSI_i : the Voltage Sensitivity Index (VSI) of the i bus; VSI_{eq} : the equivalent Voltage Sensitivity Index (VSI) of all load buses.

III. CASE STUDIES - SIMULATION AND RESULTS

The effectiveness of the proposed method is tested on the IEEE 37 bus 9 generators system [21] which is shown in Figure 5. Total the active power and the reactive power of the system are 1024.31 MW and 215.94 MVAR respectively under normal operating conditions. The maximum active power and reactive power of the system are 1087 MW and 449 MVAR. The control solutions minimize the amount of load shedding and maintain steady-state frequency from 59.7 to 60 Hz. To test the effectiveness of the proposed method, the outage situations of the generator units are calculated, simulated and tested the parameters. In the case of calculations and simulations, the spinning reserved power to control the secondary frequency is also considered. All test cases are simulated on PowerWorld GSO 19 software. The results are compared with the results of the traditional load shedding method using under frequency load shedding relay. Apply the (5), (6), (7) formulas calculate the system frequency, the amount of primary and secondary control power and the amount of load to be shed. The results of the computation of the outage generator situations are shown in Table 1.

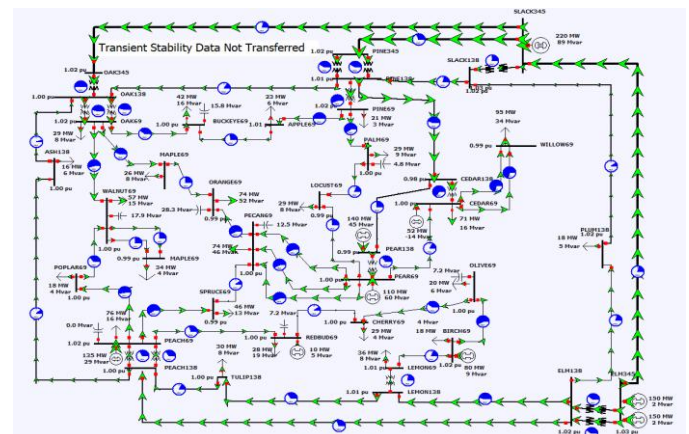


Fig. 5: The IEEE 37 bus 9 generators test system.

Table 1. The outage generators cases

Name of Gen. Bus	Frequency (Hz)	In the allow range	The primary control power value (MW)	The secondary control power value (MW)	The amount of load shedding (MW)
REDBUD	59.97	Yes	10	0	0
ELM345# 1	59.56	No	150	12.5	27.77
ELM345# 2	59.56	No	150	12.5	27.77
PEACH69	59.62	No	112.31	16.32	11.89
CEDAR69	59.86	Yes	52	0	0
BIRCH69	59.79	Yes	80	0	0

PEAR138	59.6	No	140	17.38	15.91
PEAR69	59.7	Yes	110	0	0

In the test example, the sudden disconnection of the PEAR138#1 generator (bus 53) is simulated. Applying the equation (5) calculates the stable frequency value when the PEAR138#1 generator (bus 53) disconnects from the system. The frequency value is 59.57 Hz, and shows in Figure 6.

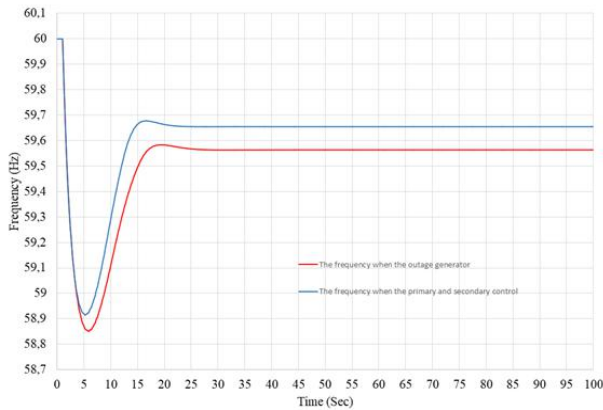


Fig. 6: The frequency of the system when the PEAR138#1 generator disconnects

After the PEAR138#1 generator suddenly disconnects, the frequency value is less than the allowable value. Therefore, the primary control and secondary frequency control which presented in section II.2 for frequency recovery should be implemented.

The primary control process is done automatically by the turbine governor after the PEAR138#1 outage generator. The value of the primary control power of each generator turbine is shown in Table 2.

Table 2. The value of the primary control power of the generators

Generator	The increased primary control power of each generator (MW)
REDBUD69 (bus 14)	5.2
ELM345#1 (bus 28)	23.6
ELM345#2 (bus 28)	23.6
SLACK345 (bus 31)	32.8
PEACH69 (bus 44)	21
CEDAR69 (bus 48)	7.5
BIRCH69 (bus 50)	11.2
PEAR138 (bus 53)	0
PEAR69 (bus 54)	15.1
Total = 140 MW	

Because the recovery frequency is less than the allowable value, so the secondary control is implemented after the primary control. The spinning reversed power of the generators will be mobilized to perform the secondary control. In this case, the secondary control power is 17.38

MW. The frequency of the system after the implementation of the secondary control is shown in Figure 6.

Thus, after performing the secondary control, the recovery frequency is 59.65 Hz and has not yet returned to the allowed value. Therefore, the final solution is load shedding. Equation (7) is applied to calculate the minimum amount of load shedding power to recover the frequency in allowable value.

$$P_{LS\ min} = \Delta P_L - \left(\frac{\Delta f_p}{\beta} \right) - \Delta P_{Secondary\ Max}$$

$$= 1.4 - \left(\frac{0.3}{0.00482 \times 60} \right) - 0.1738 = 0.1591 pu = 15.91 MW$$

After calculating the minimum load shedding power, the load shedding distribution at the load buses is calculated. The amount of load shedding at load buses based on the Voltage Sensitivity Index (VSI) value of all load buses. Calculation steps at section II.4 are applied to calculate the Voltage Sensitivity Index (VSI) value of all buses. The Voltage Sensitivity Index (VSI) value and the voltage at load bus (pu) at all load buses is shown in Figure 7.

The priority load shedding distribution for each load bus is calculated based on the following principle: The lower VSI, the greater the amount of shedding power. Equation (7) in Section II.3 is applied to calculate the amount of disconnection power value at the load buses.

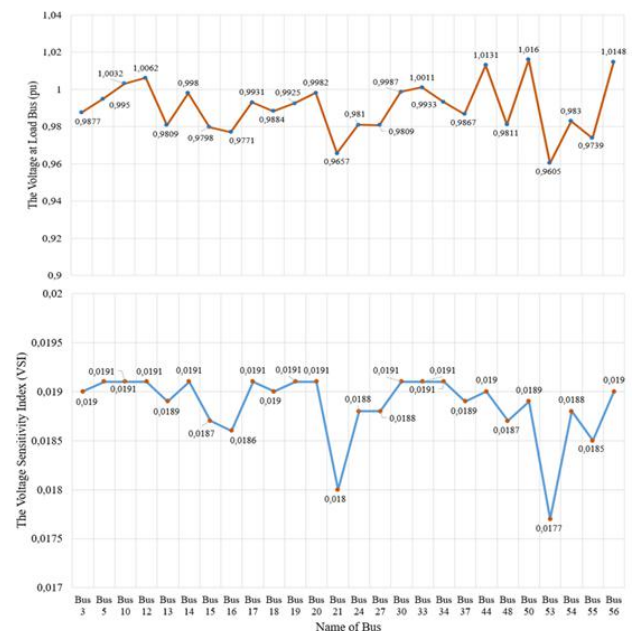


Fig.7. The VSI and the voltage at load buses (pu) after the outage generator (PEAR138)

In order to compare the effectiveness of the proposed method, the load shedding method using under frequency load shedding relay is used to compare. The process of UFLS is implemented when the frequency reduces below

the frequency setting threshold. The load is usually cut step-by-step based on the load shedding table that pre-designed based on the general rule and operator experience. These tables guide the amount of load that should be cut at each step depending on the decrease of frequency. These values are shown in Table 3.

Table 3. The UFLS scheme using load shedding table[22]

The steps UFLS	Frequency (Hz)	Time delay (s)	The amount of load shedding (the percent of total load)	Total amount of load shedding (%)
A	59.7	0.28	9	9
B	59.4	0.28	7	16
C	59.1	0.28	7	23
D	58.8	0.28	6	29
E	58.5	0.28	5	34
F	58.2	0.28	7	41
J	59.4	10	5	46

The frequency and the rotor angle comparison between the proposed method and the UFLS method are presented in Figure 8.

It can be seen that the proposed load shedding method has less the amount of shedding (76.28 MW) than the UFLS. Here, the recovery frequency value of the proposed method is lower than the UFLS method. However, this value is still within allowable parameter and acceptable range (59.7Hz). Especially, when considering the voltage value of the proposed method is equivalent to the UFLS method, although this method has less the amount of load shedding than UFLS method. This can be explained by the fact that a large load at load nodes with the lower VSI are disconnected causing the voltage to recover faster. Figure 9 and Figure 10 show that the voltage at all nodes after load shedding according to the proposed method and the UFLS method is near the same.

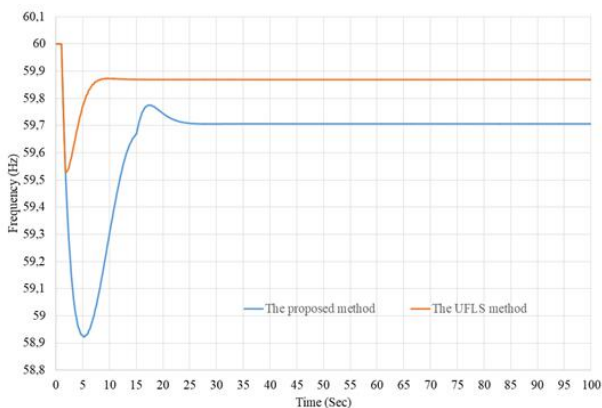


Fig. 8: The frequency comparison between the proposed method and the traditional method

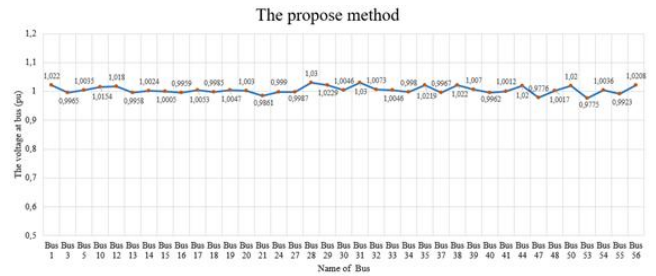


Fig.9: The voltage at all bus when load shedding according to proposed method

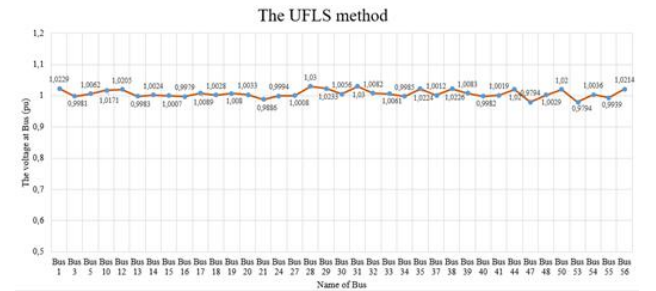


Fig.10: The voltage at all bus when load shedding according to the UFLS method

IV. CONCLUSION

A load shedding method considers to the primary and secondary control elements of the power plant to calculate the minimum amount of load shedding power and restore the frequency back to the allowable value. The proposed method ensures the frequency and voltage of the system in case of a severe generation-load mismatch. The selection of location and distribution of load shedding power at load buses are based on the Voltage Sensitivity Index (VSI) concept. The effectiveness of the proposed method has been demonstrated on a 9-machine, 37-bus system under test cases. The performance of this method is found to be better than that of a conventional UFLS scheme. The test results show that the proposed method results in reduced amount of load shedding while satisfying the operating conditions and limitations of the network.

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